

Bottlebrush Midblocks Promote Colloidal Bridging of Telechelic Polymers

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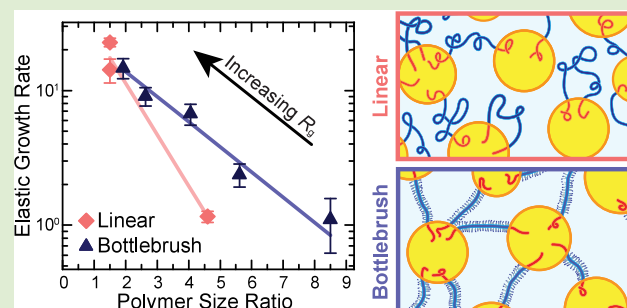


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Supporting Information

ABSTRACT: Telechelic polymers are effective rheological modifiers that bridge between associative constituents to form elastic networks. The performance of linear telechelic chains, however, is controlled by entropic forces and thus suffers from an upper limit on bridge formation. This work overcomes this limitation by utilizing telechelic triblock copolymers containing bottlebrush midblocks. By comparing the rheological properties of emulsions linked by telechelic bottlebrush polymers to those containing linear chains, we determined that telechelic polymers with bottlebrush midblocks form elastic networks more efficiently. These enhanced rheological properties arise from the high stiffness of the bottlebrush midblocks, which offsets the entropic stretching penalty for bridge formation, enabling them to more readily form networks. This molecular-level control over polymer conformation in complex fluids opens avenues for designing highly elastic networks with minimal polymeric additives.



Telechelic polymers contain reactive or associative endgroups that facilitate their self-assembly in melts,^{1–4} in solution,^{5–11} and in the presence of constituents such as colloidal suspensions^{12–15} or emulsions.^{16–20} This self-assembly depends on both solvent choice and polymer molecular weight M_w . When dispersed in a midblock-selective solvent, the endgroups of telechelic polymers can associate with themselves to micellize^{7,9,10,21} or with neighboring chains to form a network.^{5,11,22} Network formation can be enhanced through the inclusion of associative constituents, such as colloids or emulsions,^{20,23,24} in which the functional endgroups of the telechelic chains enthalpically associate with the particle surfaces or partition into dispersed droplets, while the midblock remains in the continuous phase. Each chain will thus adopt one of two conformations: a loop with both endgroups coordinating with the same constituent particle or a bridge with each endgroup coordinating with a distinct particle. Because loops serve as defects,^{25,26} the properties of the resulting network depend on the ratio at which the polymers form bridges versus loops. In contrast to block copolymer melts where structure emerges from geometric constraints and evolves thermodynamically,^{27,28} the structure of suspensions is dictated by the constituent size and volume fraction. Thus, there remain open questions of how telechelic block copolymers couple to this amorphous structure and how control over this interplay can drive the system to a highly bridged state by minimizing loop formation.

Telechelic polymers with low molecular weight M_{end} endblocks form viscoelastic networks in colloidal systems^{19,29–31} because the weak associations exist in a dynamic

equilibrium that facilitates relaxations.^{32,33} Alternatively, chains with large M_{end} generate highly elastic gels because the endblocks irreversibly associate, forming kinetically trapped systems that resist thermal fluctuations.^{20,24} While M_{end} controls network relaxations, midblock M_w (M_{mid}) controls the bridging fraction $\epsilon = n_B/n_T$, where n_B and n_T are the number densities of bridging chains and total chains, respectively. Previous simulation work on polymer-linked colloids has shown that bridging is entropically controlled according to the ratio of the surface-to-surface distance D_{ID} to midblock radius of gyration $R_{g,mid}$.^{34–36} At a large D_{ID} or small $R_{g,mid}$, polymers must undergo entropically unfavorable stretching to interact with neighboring particles and therefore preferentially adopt loop conformations. By contrast, for small D_{ID} or large $R_{g,mid}$ the chains require only minor deformations to interact with neighboring particles, and the bridging becomes governed by the statistical probability. As $D_{ID}/R_{g,mid} \rightarrow 0$, ϵ approaches a maximum of approximately 1/3, arising from the statistics of there being two independent combinations to form a loop but only one to form a bridge, which presents a significant limitation on the use of telechelic polymers as rheological modifiers.

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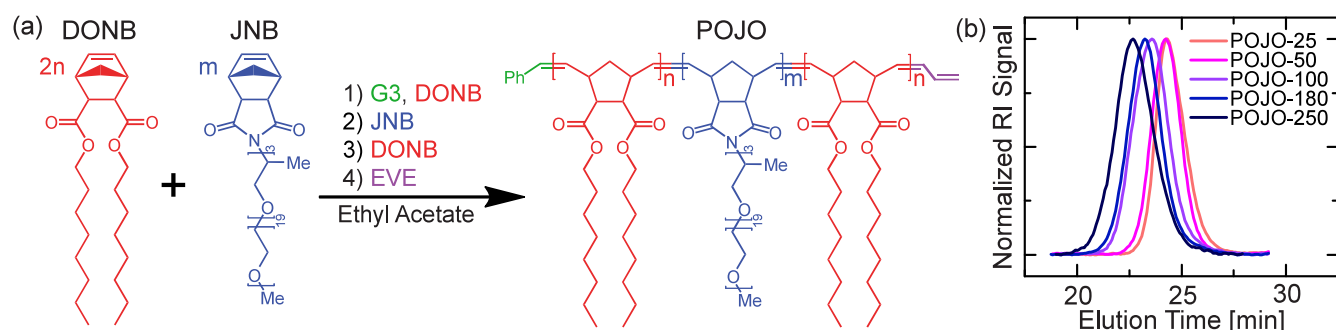


Figure 1. (a) Synthesis scheme of the POJO telechelic triblock copolymer from dioctyl dicarboxylic norbornene (DONB) and Jeffamine M-1000 norbornene (JNB). (b) Normalized refractive index (RI) signal as a function of elution time for POJO with varying M_{mid} .

In this Letter, we improve the bridging efficiency by introducing an entropic penalty for loop formation through the use of telechelic triblock copolymers with bottlebrush midblocks. The pendant sidechains of bottlebrush polymers introduce steric hindrance along the backbone, increasing the midblock persistence length^{37–39} and spatially separating the endblocks. The size and rigidity of bottlebrush polymers depends on the degree of polymerization of both the backbone N_{bb} and sidechains N_{sc} as well as the sidechain grafting density.^{38,40–57} Here, we synthesize telechelic triblock copolymers with bottlebrush midblocks and linear endblocks through ring-opening metathesis polymerization (ROMP) to create a library of polymers with varying M_{mid} and constant M_{end} . We use these copolymers to link emulsions into elastic networks, and by comparing the dependence of emulsion elasticity on the normalized length scale $D_{\text{ID}}/R_{\text{g, mid}}$, we find that polymers with bottlebrush midblocks exhibit a quantitatively higher relative bridging fraction ϵ compared with those with linear midblocks. Our findings demonstrate that by tailoring polymer topology, we can modify the coupling of polymer conformation to the structure of complex fluids, resulting in highly bridged, elastic networks.

The polymer-linked emulsions (PLEs) must satisfy two key criteria. First, the continuous and dispersed phases must be immiscible and minimally volatile. Second, the telechelic triblock copolymers must have orthogonally soluble blocks such that the endblocks partition into the oil droplets and the midblocks into the continuous phase. To satisfy these requirements, we use ROMP to synthesize triblock copolymers containing hydrophobic poly(dioctyl dicarboxylic norbornene) endblocks⁵⁸ and bottlebrush midblocks of poly(Jeffamine M-1000 norbornene)⁵⁹ – a norbornene group functionalized with a hydrophilic polyetheramine of $N_{\text{sc}} \approx 22$ with repeating units of propylene oxide and ethylene oxide (Figure 1a). Based on established scaling laws,⁶⁰ we estimate that the Jeffamine M-1000 side chains have a radius of gyration $R_{\text{g}} \approx 1$ nm, leading to a persistence length $l_{\text{p}} \approx 2R_{\text{g}} \approx 2$ nm.^{37,61} The synthesis employs a one-pot ROMP procedure⁶² initiated by Grubb's third generation catalyst⁶³ (G3) with the sequential addition of macromonomers and termination by ethyl vinyl ether (EVE). M_{end} is held constant at 34 ± 5 kDa to achieve effectively irreversible endblock partitioning,^{20,24} and M_{mid} is varied from 25 to 250 kDa (equivalent to $N_{\text{bb}} \approx 21$ –210) to test midblocks with conformations ranging from star-like ($N_{\text{bb}} \approx N_{\text{sc}}$) to worm-like chains ($N_{\text{bb}} \gg N_{\text{sc}}$).⁴⁸ Furthermore, there is a practical upper limit on M_{mid} because of the challenges in losing catalyst activity from monomer coordination or residual impurities. The M_{w} and dispersity \mathcal{D} of the poly(dioctyl

dicarboxylic norbornene)-*b*-poly(Jeffamine M-1000 norbornene)-*b*-poly(dioctyl dicarboxylic norbornene) (POJO) triblock copolymers are detailed in Table 1, and GPC elution

Table 1. Polymer Nomenclature, Target Weight-Average Molecular Weight M_{w} of the Midblock and Endblocks, Total Measured M_{w} , and Measured Dispersity \mathcal{D} of the POJO Polymers

polymer	target midblock M_{w} (kDa)	target endblocks M_{w} (kDa)	total M_{w} (kDa)	\mathcal{D}
POJO-25	25	30	80.7	1.36
POJO-50	50	30	97.8	1.31
POJO-100	100	30	176.5	1.45
POJO-180	180	30	218.8	1.58
POJO-250	250	30	332.0	1.74

curves are shown in Figure 1b. Additional synthesis details are provided in the Supporting Information. The POJO polymers were added to 1-decanol-in-water emulsions at nominal concentrations of 0.25 to 3 wt %, corresponding to molar concentrations ranging from 0.012 to 0.48 mmol/L depending on M_{mid} . Specific concentrations are detailed in the Supporting Information. At concentrations above ~ 3 wt %, samples appear heterogeneous as a result of polymer insolubility or insufficient mixing, setting an upper bound for the testable concentrations. The emulsions have droplet diameters $d_{\text{H}} = 400$ nm, as determined by DLS (Supporting Information) and a volume fraction $\phi = 0.5$. Rheological properties are characterized on a TA Instruments HR-20 Rheometer using 2° cone-and-plate geometries with diameters of 20 and 60 mm, respectively, and a gap height of 54 μm .

We characterize the PLE rheology as a function of both oscillation amplitude γ and oscillation frequency ω (Figure 2). While the neat emulsions are dominated by liquid-like behavior (Supporting Information), we observe a dramatic increase in emulsion elasticity upon the addition of POJO, with dependencies on both polymer concentration c and M_{mid} . The PLEs are elastic in the linear viscoelastic region (i.e., $\gamma \lesssim 0.6\%$) with the storage modulus G' greater than the loss modulus G'' , and they exhibit the typical signs of yielding for Type III materials⁶⁴ as γ is further increased, with the appearance of a maximum in G'' , a crossover between G' and G'' , and a subsequent decay in both moduli (Figure 2a). PLEs with higher c or M_{mid} typically display greater moduli and larger overshoots in G'' ,^{65–67} suggesting that increased n_{B} promotes the formation of more cohesive elastic networks.

We additionally examined the system through linear frequency sweeps, measuring G' and G'' as a function of ω

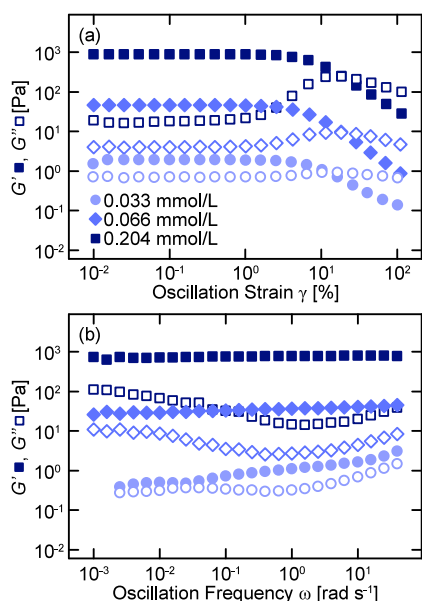


Figure 2. Storage modulus G' (closed) and loss modulus G'' (open) as a function of (a) strain amplitude γ at a fixed frequency $\omega = 10 \text{ rad s}^{-1}$ and (b) as a function of frequency ω at a fixed amplitude $\gamma = 0.3\%$ for emulsions containing POJO-180 of varying concentrations c .

(Figure 2b). For nearly all c and M_{mid} , the PLEs are elastic with $G' > G''$ across all experimentally accessible ω . Furthermore, G' becomes nearly independent from ω at higher c , characteristic of soft, glassy materials^{68,69} and indicating that large-scale viscous rearrangements are suppressed. This glassy-like rheology is further supported by the presence of a minimum in G'' centered at $\omega \approx 1 \text{ rad s}^{-1}$. The upturn in G'' at higher frequencies reflects contributions from rapid relaxations of individual polymer segments,⁷⁰ and the increase at lower frequencies corresponds to slow structural relaxations. Unlike standard Maxwellian descriptions of viscoelasticity,^{71,72} G' and G'' do not display a crossover even as ω approaches $10^{-3} \text{ rad s}^{-1}$, demonstrating that the endblocks are strongly partitioned into the dispersed droplets and kinetically trapped by enthalpic forces. We observe qualitatively similar frequency and concentration dependencies regardless of M_{mid} with decreasing M_{mid} resulting in similar effects as decreasing c (Supporting Information).

To further explore the network formation of the telechelic bottlebrushes, we examined the PLE elasticity at a fixed frequency $\omega = 10 \text{ rad s}^{-1}$ as a function of c (Figure 3). For all M_{mid} , increasing c leads to larger G' and smaller $\tan(\delta) = G''/G'$ due to a greater bridging density n_B . Polymers with larger M_{mid} form cohesive networks more rapidly, consistent with earlier findings on linear telechelic polymers.^{20,35,36} Although both linear and bottlebrush telechelic polymers produce elastic networks, PLEs formed by linear polymers²⁰ display a plateau at $\tan(\delta) \approx 10^{-1}$ whereas the bottlebrush PLEs approach $\tan(\delta) \approx 10^{-2}$ at the highest c and M_{mid} . These low values of $\tan(\delta)$ suggest that the POJO chains contribute more specifically to network elasticity with minimal viscous dissipation, which may result from fewer relaxation modes in the bottlebrush midblocks.

These rheological dependencies on c can be quantified by fitting each curve to a modified Langmuir isotherm, given by

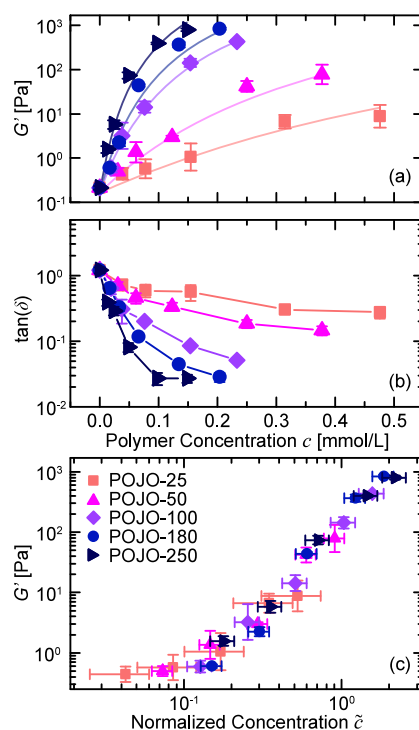


Figure 3. (a) Storage modulus G' and (b) loss tangent $\tan(\delta)$ as a function of polymer concentration c at $\omega = 10 \text{ rad s}^{-1}$. Curves in (a) are fits to eq 1 and in (b) are guides to the eye. (c) Storage modulus G' as a function of normalized polymer concentration $\tilde{c} = mc$. Error bars in y are one log-normal standard deviation, and error bars in x are 95% confidence intervals on the fitting parameter m .

$$G = G_0 \exp\left(\frac{Kmc}{1 + mc}\right) \quad (1)$$

where $G_0 = 0.16 \pm 0.02 \text{ Pa}$ is the storage modulus of the neat emulsion, K is a constant related to the elasticity of the emulsion at the high- c plateau, and m characterizes the increase in emulsion elasticity per mole of polymer in the low- c limit. We assume that network properties at infinite c are controlled by the size and volume fraction of the emulsion droplets and therefore restrict K to be constant across the samples. A global fit on K finds $K = 13.0 \pm 0.7$, corresponding to a limiting plateau $G' = G_0 \exp(K) \approx 70 \text{ kPa}$. Although largely empirical, this fit successfully captures the initial exponential increase and eventual plateau in elasticity across all c and M_{mid} . By defining a normalized concentration $\tilde{c} = cm$, we collapse G' onto a master curve for all M_{mid} (Figure 3c), demonstrating that the mechanisms by which these telechelic polymers form networks is preserved across all M_{mid} . We hypothesize that the sigmoidal growth in elasticity (Figure 3c) emerges from an interplay of physical phenomena, as follows: (1) the plateau in G' at low \tilde{c} corresponds to the finite elasticity of the neat emulsion, (2) the rise in G' occurs as bridging chains induce percolation between droplets,^{14,73–76} and (3) the high- \tilde{c} plateau in G' arises as polymers saturate the droplet surfaces and begin to form redundant bridges. A precise theoretical description of these physics, however, remains elusive due to the challenging physics of this system. Because the interaction range in PLEs is on the order of $R_{\text{g, mid}}$, the PLE system violates the assumption underlying existing theories for suspensions of attractive colloids that the interaction range is significantly smaller than the particle size.^{77–79} Furthermore, mean-field theories, such as

the affine network model,⁷¹ severely underestimate the moduli of these PLEs, which we attribute to the heterogeneous structure of the system. Additional theoretical advances are therefore needed to mechanistically describe these complex systems beyond our empirical model.

Nevertheless, this empirical fit provides a framework to describe the elastic growth by quantifying the initial rate of change in G' in a single parameter m . We posit that m captures the increase in elasticity per chain, which is directly proportional to the product of the bridging fraction and strength of endblock partitioning²⁰ according to $m \sim \varepsilon \mathcal{F}(M_{\text{end}})$. Therefore, telechelic polymers with different endblocks are expected to have different values for $\mathcal{F}(M_{\text{end}})$ but similar dependencies on m . To isolate contributions from ε , we quantify the dependence of m on the normalized distance $D_{\text{ID}}/R_{\text{g,mid}}$ for telechelic chains with either bottlebrush or linear midblocks (Figure 4), where $D_{\text{ID}} = d_{\text{H}}[(\phi_{\text{max}}/\phi)^{1/3} - 1] \approx$

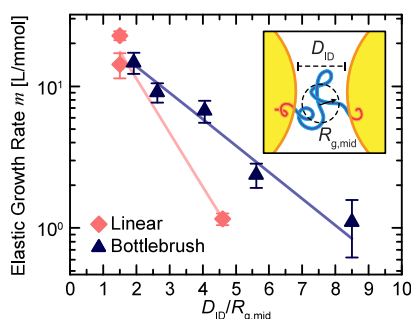


Figure 4. Elastic growth rate m as a function of the ratio of interdroplet distance to midblock radius of gyration $D_{\text{ID}}/R_{\text{g,mid}}$ for POJO (this work) and SEOS (ref 20) polymers. Curves are exponential fits. Inset: Schematic illustrating D_{ID} and $R_{\text{g,mid}}$.

34 nm is the surface-to-surface distance between droplets,⁸⁰ $\phi_{\text{max}} = 0.64$ corresponds to random close packing, and $R_{\text{g,mid}}$ is the radius of gyration of homopolymers of the midblock determined from intrinsic viscosity measurements (Supporting Information). For both systems, we observe that m decreases exponentially with increasing $D_{\text{ID}}/R_{\text{g,mid}}$ according to $m \sim \exp(-aD_{\text{ID}}/R_{\text{g,mid}})$, where a characterizes the decay rate. For linear polymers, $a = 0.93 \pm 0.10$, while for bottlebrush polymers, $a = 0.44 \pm 0.05$. By comparing the decay rates a rather than m , we remove effects arising from the different endblock chemistries to quantify the effect of the normalized distance on the bridging fraction ε . For example, we identify that for linear polymers, m decays over an order of magnitude from $D_{\text{ID}}/R_{\text{g,mid}} \approx 1$ to 4.7 whereas in bottlebrush systems, m decreases a similar amount only when $D_{\text{ID}}/R_{\text{g,mid}} \approx 8.5$. This difference in bridging propensity over larger distances indicates that the high stiffness of the bottlebrush midblock and subsequent spatial separation of the endblocks enhance bridge formation and prevent the dramatic decline in elasticity observed for linear polymers. While a provides insight into the decay rate of the bridging fraction, we cannot comment on the exact values of ε in each system. To the best of our knowledge, no experimental technique can currently distinguish between bridging and looping chains in these classes of complex fluids, despite previous observations in polymer networks,⁸¹ solutions,⁸² suspensions,⁸³ and melts.^{4,84–88} Thus, resolving even relative bridging densities solves a critical knowledge gap in polymer physics and enables direct

comparisons of the efficacy of different polymer chemistries and topologies.

We also note that this normalization $D_{\text{ID}}/R_{\text{g,mid}}$ already accounts for the larger sizes of bottlebrush polymers at comparable degrees of polymerization, and thus, the enhanced bridging of bottlebrushes is not simply a size effect. Instead, we attribute this enhanced bridging capability to two primary mechanisms. First, the longer persistence length of the bottlebrush midblocks ($l_p \approx 2$ nm) introduces an entropic penalty for loop formation. Second, the worm-like nature of the chains leads to spatially localized endblocks, quantified by a nonzero average end-to-end vector.⁸⁹ Although the large persistence lengths and worm-like chain behavior of bottlebrush polymers have been well-established in the literature, the effects of these conformational characteristics on the bridging behavior in colloidal systems have not been explored. In melts, triblock bottlebrush polymers can readily form loops as they orient parallel to interfaces, even decreasing the bridging fraction relative to linear polymers.^{4,90} This melt behavior contrasts with the behavior of telechelic bottlebrushes in suspensions observed here, which we attribute to length scales in suspensions being set by particle size and volume fraction rather than by the relative fractions of each block. Additionally, phase separation proceeds thermodynamically in a melt, but partitioning is primarily controlled by the kinetics in these emulsions. We expect that this combination of kinetically controlled association and coupling between the polymer conformation and emulsion structure plays a dominant role in the enhanced bridging fraction achieved by bottlebrush midblocks.

Our work demonstrates that telechelic triblock copolymers are effective rheological modifiers, capable of bridging between emulsion droplets to form elastic networks. We synthesized triblock copolymers with bottlebrush midblocks at different degrees of polymerization via ROMP, and we utilized these polymers to assemble emulsions into elastic networks. The resulting polymer-linked emulsions display unique rheological behavior with suppressed terminal relaxations and high elasticities that can be collapsed onto a single master curve according to the elastic growth rate m . Although the exponential scaling of elasticity does not follow existing theoretical predictions, we show that this growth rate m is directly related to the bridging fraction ε and facilitates a quantitative comparison of bridging between different polymer chemistries. We observe significantly greater bridge formation for bottlebrush midblocks than for linear midblocks, indicating that stiffer midblocks promote bridging by imposing an entropic penalty for loop formation and spatially separating endblocks. Our results suggest that modulating the structure and conformations of telechelic block copolymers is a promising approach to tune their bridging ability. This demonstrated control opens a broad swath of opportunities to design dynamic complex fluids that can improve processability and performance in advanced manufacturing,⁹¹ respond to environmental stimuli to drive controlled transport,²³ or exhibit biomimetic properties for tissue engineering and biomanufacturing.⁹²

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsmacrolett.4c00428>.

Experimental section, intrinsic viscosity measurements, synthesis details, polymer and emulsion details, neat emulsion characterization, additional rheological data, information on fitting methods, and calculations (PDF)

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Author Contributions

CRedit: **Daniel P. Keane** conceptualization, data curation, formal analysis, investigation, methodology, validation, writing - original draft, writing - review & editing; **Timea Kolozsvary** methodology, writing - review & editing; **Benjamin McDonald** conceptualization, funding acquisition, project administration, resources, supervision, writing - review & editing; **Ryan Poling-Skutvik** conceptualization, funding acquisition, project administration, resources, supervision, writing - original draft, writing - review & editing.

Notes

The authors declare no competing financial interest.

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